

UNIQUE STUDY POINT

BY SUMEET SAHU

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Class: X	Subject: Mathematics	Session: 2025-26
Chapter: Ch 10: Circles (PYQ)		

PREVIOUS YEAR QUESTIONS (PYQ)

Chapter 10: Circles

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This document contains chapter-wise Previous Year Questions from CBSE Class X Board Examinations (2019-2025) for **Chapter 10: Circles**. Each question includes the year of examination, marks allotted, and direct answer for quick revision.

△ NOTE: As per CBSE 2025-26 Syllabus. Topics: Tangent to a circle at point of contact, (Prove) Tangent \perp Radius, (Prove) Equal tangents from external point. No deletions.

SECTION A: Multiple Choice Questions (1 Mark Each)

[CBSE 2024 | 1 Mark]

Q1. The maximum number of common tangents that can be drawn to two circles intersecting at two distinct points is:

- (a) 4
- (b) 3
- (c) 2
- (d) 1

Ans: (c) 2. Two circles intersecting at two points have exactly 2 common tangents.

[CBSE 2024 | 1 Mark]

Q2. In the figure, PT is tangent to a circle with centre O and $\angle TPO = 35^\circ$. The measure of $\angle x$ (exterior angle at O) is:

- (a) 110°
- (b) 115°
- (c) 120°
- (d) 125°

Ans: (d) 125° . $\angle OTP = 90^\circ$ (tangent \perp radius). $\angle x = \angle TPO + \angle OTP = 35^\circ + 90^\circ = 125^\circ$ (exterior angle).

[CBSE 2024 | 1 Mark]

Q3. O is the centre of the circle. MN is a chord and tangent ML at point M makes an angle of 70° with MN. The measure of $\angle MON$ is:

- (a) 120°
- (b) 130°
- (c) 140°
- (d) 150°

Ans: (c) 140° . $\angle OML = 90^\circ \Rightarrow \angle OMN = 90^\circ - 70^\circ = 20^\circ$. $OM = ON$ (radii) $\Rightarrow \angle ONM = 20^\circ$. $\angle MON = 180^\circ - 40^\circ = 140^\circ$.

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[CBSE 2023 | 1 Mark]

Q4. PT is a tangent at T to the circle with centre O. If $\angle TPO = 25^\circ$, then $\angle x$ (angle at O in $\triangle OTP$ extended) is:

- (a) 25°
- (b) 65°
- (c) 90°
- (d) 115°

Ans: (d) 115° . $\angle PTO = 90^\circ$. By exterior angle: $x = 90^\circ + 25^\circ = 115^\circ$.

[CBSE 2023 | 1 Mark]

Q5. PQ is tangent to circle centred at O. If $\angle AOB = 95^\circ$, the measure of $\angle ABQ$ is:

- (a) 47.5°
- (b) 42.5°
- (c) 85°
- (d) 95°

Ans: (a) 47.5° . $OA = OB$ (radii). $\angle OAB = \angle OBA = (180^\circ - 95^\circ)/2 = 42.5^\circ$. $\angle OBQ = 90^\circ \Rightarrow \angle ABQ = 90^\circ - 42.5^\circ = 47.5^\circ$.

[CBSE 2022 | 1 Mark]

Q6. From an external point Q, the length of tangent to a circle is 24 cm and distance of Q from the centre is 25 cm. The radius of the circle is:

- (a) 5 cm
- (b) 7 cm
- (c) 12 cm
- (d) 15 cm

Ans: (b) 7 cm. $r = \sqrt{(25^2 - 24^2)} = \sqrt{(625 - 576)} = \sqrt{49} = 7$ cm.

[CBSE 2021 | 1 Mark]

Q7. If two tangents inclined at an angle of 60° are drawn to a circle of radius 3 cm, then the length of each tangent is:

- (a) 3 cm
- (b) $3\sqrt{3}$ cm
- (c) 6 cm
- (d) $3\sqrt{3}/2$ cm

Ans: (b) $3\sqrt{3}$ cm. Half angle = 30° . $\tan 30^\circ = r/\text{tangent} \Rightarrow 1/\sqrt{3} = 3/T \Rightarrow T = 3\sqrt{3}$ cm.

[CBSE 2020 | 1 Mark]

Q8. In the figure, PA and PB are tangents from P to circle with centre O. If $\angle APB = 60^\circ$, then $\angle AOB$ is:

- (a) 60°
- (b) 90°
- (c) 120°
- (d) 150°

Ans: (c) 120° . $\angle APB + \angle AOB = 180^\circ$ (supplementary in quad OAPB). $\angle AOB = 180^\circ - 60^\circ = 120^\circ$.

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[CBSE 2019 | 1 Mark]

Q9. AP, AQ and BC are tangents to a circle with centre O. If AB = 5 cm, AC = 6 cm and BC = 4 cm, then the length of AP is:

- (a) 15 cm
- (b) 10 cm
- (c) 9 cm
- (d) 7.5 cm

Ans: (d) 7.5 cm. AP = AQ. Let BP = x, then CQ = BC - x. AP = AB + BP = 5 + x. AQ = AC + CQ = 6 + (4 - x). AP = AQ ⇒ 5 + x = 10 - x ⇒ 2x = 5 ⇒ x = 2.5. AP = 7.5 cm.

[CBSE 2019 | 1 Mark]

Q10. A circle can have _____ parallel tangents at the most.

- (a) 0
- (b) 1
- (c) 2
- (d) Infinite

Ans: (c) 2. Only at the ends of a diameter can parallel tangents be drawn.

SECTION B: Assertion-Reason Questions (1 Mark Each)

[CBSE 2024 | 1 Mark]

Q11. Assertion (A): The tangent at any point of a circle is perpendicular to the radius through the point of contact.

Reason (R): The shortest distance from a point to a line is the perpendicular distance.

- (a) Both true, R explains A
- (b) Both true, R does not explain A
- (c) A true, R false
- (d) A false, R true

Ans: (a) Both true and R explains A. The radius is the shortest distance from centre to tangent, hence perpendicular.

[CBSE 2023 | 1 Mark]

Q12. Assertion (A): Two tangents drawn from an external point to a circle are equal in length.

Reason (R): In two right triangles, if the hypotenuse and one side are equal, the triangles are congruent (RHS).

- (a) Both true, R explains A
- (b) Both true, R does not explain A
- (c) A true, R false
- (d) A false, R true

Ans: (a) Both true and R explains A. The proof uses RHS congruence of $\triangle OPA \cong \triangle OPB$.

SECTION C: Short Answer Questions (2 Marks Each)

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[CBSE 2022 | 2 Marks]

Q13. Prove that the tangents drawn at the ends of a diameter of a circle are parallel.

Ans: Let AB be diameter. Tangent PQ at A: $\angle OAP = 90^\circ$. Tangent RS at B: $\angle OBR = 90^\circ$. Since $\angle OAP = \angle OBR = 90^\circ$ (alternate interior angles with transversal AB), $PQ \parallel RS$.

[CBSE 2023 | 2 Marks]

Q14. Two concentric circles are of radii 5 cm and 3 cm. Find the length of the chord of the larger circle which touches the smaller circle.

Ans: AB is chord of larger circle, tangent to smaller at P. $OP \perp AB$, $OP = 3$, $OA = 5$. $AP = \sqrt{(25-9)} = 4$ cm. $AB = 2 \times AP = 8$ cm.

[CBSE 2021 | 2 Marks]

Q15. In the figure, O is the centre of a circle, PQ is a chord and PT is the tangent at P. If $\angle POQ = 70^\circ$, find $\angle TPQ$.

Ans: $\angle OPQ = \angle OQP = (180^\circ - 70^\circ)/2 = 55^\circ$ (isosceles \triangle , $OP = OQ$). $\angle OPT = 90^\circ$ (tangent \perp radius). $\angle TPQ = 90^\circ - 55^\circ = 35^\circ$.

[CBSE 2020 | 2 Marks]

Q16. Find the perimeter of a square circumscribing a circle of radius a cm.

Ans: Side of square = diameter = $2a$ cm. Perimeter = $4 \times 2a = 8a$ cm.

SECTION D: Short Answer Questions (3 Marks Each)

[CBSE 2024 | 3 Marks]

Q17. Prove that the angle between the two tangents drawn from an external point to a circle is supplementary to the angle subtended by the line segment joining the points of contact at the centre.

Ans: Let PA, PB be tangents from P. $\angle OAP = \angle OBP = 90^\circ$ (tangent \perp radius). In quadrilateral OAPB: $\angle OAP + \angle APB + \angle OBP + \angle AOB = 360^\circ$. $90^\circ + \angle APB + 90^\circ + \angle AOB = 360^\circ$. $\angle APB + \angle AOB = 180^\circ$. Hence supplementary.

[CBSE 2023 | 3 Marks]

Q18. Two tangents TP and TQ are drawn to a circle with centre O from an external point T. Prove that $\angle PTQ = 2\angle OPQ$.

Ans: Let $\angle PTQ = \theta$. $TP = TQ$ (tangents). $\triangle TPQ$ is isosceles. $\angle TPQ = \angle TQP = (180^\circ - \theta)/2 = 90^\circ - \theta/2$. $\angle OPT = 90^\circ$ (tangent \perp radius). $\angle OPQ = \angle OPT - \angle TPQ = 90^\circ - (90^\circ - \theta/2) = \theta/2$. So $\angle PTQ = 2\angle OPQ$. Hence proved.

[CBSE 2022 | 3 Marks]

Q19. A circle is inscribed in a $\triangle ABC$ with sides $AB = 8$ cm, $BC = 6$ cm and $AC = 10$ cm. The circle touches AB, BC and CA at P, Q and R respectively. If $\angle B = 90^\circ$, find the radius of the incircle.

Ans: OPBQ is a square (since $\angle B = 90^\circ$ and $OP \perp AB$, $OQ \perp BC$). Let $r =$ radius. $BP = BQ = r$. $AP = AR = 8 - r$. $CQ = CR = 6 - r$. $AC = AR + CR \Rightarrow 10 = (8 - r) + (6 - r) = 14 - 2r \Rightarrow 2r = 4 \Rightarrow r = 2$ cm.

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[CBSE 2021 | 3 Marks]

Q20. Two concentric circles are of radii 7 cm and r cm ($r > 7$). A chord of the larger circle of length 48 cm touches the smaller circle. Find the value of r .

Ans: $OC = 7$ cm (radius of smaller). $AB = 48$ cm (chord). $OC \perp AB$ (tangent). $AC = 24$ cm. In rt. $\triangle OCA$: $r^2 = 7^2 + 24^2 = 49 + 576 = 625 \Rightarrow r = 25$ cm.

SECTION E: Long Answer Questions (4-5 Marks Each)

[CBSE 2024 | 5 Marks]

Q21. Prove that the lengths of tangents drawn from an external point to a circle are equal.

Ans: Given: Circle with centre O , external point P , tangents PA and PB . To prove: $PA = PB$. Proof: In $\triangle OPA$ and $\triangle OPB$: $OA = OB$ (radii), $OP = OP$ (common), $\angle OAP = \angle OBP = 90^\circ$ (tangent \perp radius). By RHS: $\triangle OPA \cong \triangle OPB$. Therefore $PA = PB$ (CPCT). Hence proved.

[CBSE 2023 | 5 Marks]

Q22. Prove that a parallelogram circumscribing a circle is a rhombus.

Ans: Let $ABCD$ be a parallelogram circumscribing a circle. Tangent lengths from each vertex: $AP = AS$, $BP = BQ$, $CQ = CR$, $DR = DS$. $AB + CD = (AP+BP) + (CR+CQ) = (AS+DS) + (BQ+CQ) = AD + BC$. But $AB = CD$, $AD = BC$ (parallelogram). So $AB + AB = AD + AD \Rightarrow AB = AD$. All sides equal $\Rightarrow ABCD$ is a rhombus.

[CBSE 2021 | 5 Marks]

Q23. Prove that opposite sides of a quadrilateral circumscribing a circle subtend supplementary angles at the centre.

Ans: Let $ABCD$ circumscribe circle with centre O touching at P, Q, R, S . Join OP, OQ, OR, OS . In $\triangle OAP$ and $\triangle OAS$: $AP = AS$, $OP = OS$, $OA = OA \Rightarrow \triangle OAP \cong \triangle OAS$. So $\angle 1 = \angle 2$. Similarly pair all 8 angles at centre. Sum = $2(\angle 1 + \angle 3 + \angle 5 + \angle 7) = 360^\circ \Rightarrow \angle 1 + \angle 3 + \angle 5 + \angle 7 = 180^\circ$. $\angle AOB + \angle COD = 180^\circ$ and $\angle BOC + \angle AOD = 180^\circ$. Hence proved.

[CBSE 2020 | 5 Marks]

Q24. In the figure, PQ is a chord of length 16 cm of a circle of radius 10 cm. The tangents at P and Q intersect at T . Find the length of TP .

Ans: Let $TR \perp PQ$ at R (perpendicular bisector). $PR = 8$ cm. In rt. $\triangle PRO$: $OR = \sqrt{(10^2 - 8^2)} = 6$ cm. Let $TP = x$, $TR = y$. $OT = y+6$. In rt. $\triangle PRT$: $x^2 = y^2 + 64$... (i). In rt. $\triangle OPT$: $(y+6)^2 = x^2 + 100 \Rightarrow y^2 + 12y + 36 = y^2 + 64 + 100 \Rightarrow 12y = 128 \Rightarrow y = 32/3$. $x^2 = (32/3)^2 + 64 = 1024/9 + 576/9 = 1600/9 \Rightarrow x = 40/3$ cm.

SECTION F: Case Study Based Questions (4 Marks Each)

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[CBSE 2025 | 4 Marks]

Q25. Case Study: A circle is inscribed in a $\triangle PQR$ with $PQ = 10$ cm, $QR = 8$ cm, $PR = 12$ cm. The circle touches PQ at A , QR at B and PR at C .

- (i) If $PA = x$, find QA in terms of x .
- (ii) Find QB in terms of x .
- (iii) Find the value of x .
- (iv) Find the lengths PA , QB and RC .

Ans: $PA = PC = x$ (tangents from P). $QA = PQ - PA = 10 - x$. $QB = QA = 10 - x$ (tangents from Q). $RB = QR - QB = 8 - (10 - x) = x - 2$. $RC = RB = x - 2$ (tangents from R). $PR = PC + RC \Rightarrow 12 = x + (x - 2) \Rightarrow 12 = 2x - 2 \Rightarrow x = 7$. $PA = 7$ cm, $QB = 3$ cm, $RC = 5$ cm.

[CBSE 2024 | 4 Marks]

Q26. Case Study: Two tangents PA and PB are drawn from external point P to a circle with centre O and radius 5 cm. The distance $OP = 13$ cm.

- (i) Find the length of tangent PA .
- (ii) Find $\angle OAP$.
- (iii) If $\angle APB = 60^\circ$, find $\angle AOB$.
- (iv) Find the area of $\triangle OPA$.

Ans: (i) $PA = \sqrt{(13^2 - 5^2)} = \sqrt{(169 - 25)} = \sqrt{144} = 12$ cm. (ii) $\angle OAP = 90^\circ$ (tangent \perp radius). (iii) $\angle AOB = 180^\circ - \angle APB = 180^\circ - 60^\circ = 120^\circ$ (supplementary). (iv) Area $\triangle OPA = \frac{1}{2} \times OA \times PA = \frac{1}{2} \times 5 \times 12 = 30$ cm².

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★ PYQ SUMMARY & ANALYSIS

Topic	Years Asked	Frequency	Marks
Tangent \perp Radius (angle problems)	2019–2025	Every Year	1–3
Equal tangents from external point (Proof)	2019–2025	Every Year	3–5
$\angle APB + \angle AOB = 180^\circ$ (supplementary)	2019–2025	Every Year	1–3
Length of tangent ($\sqrt{\quad}$ formula)	2019–2024	5 times	1–2
Incircle of triangle (find radius)	2019–2024	4 times	3–5
Parallelogram circumscribing = Rhombus	2019–2024	4 times	5
Concentric circles (chord touches inner)	2019–2023	3 times	2–3
Case Study (tangent properties)	2024–2025	2 times	4

Key Observations for Students:

- ✓ THEOREM 1: Tangent \perp Radius at point of contact — used in EVERY tangent problem.
- ✓ THEOREM 2: Tangents from external point are equal ($PA = PB$) — MUST know proof (RHS congruence).
- ✓ $\angle APB + \angle AOB = 180^\circ$ — very frequent MCQ/short answer.
- ✓ Length of tangent from external point: $T = \sqrt{(d^2 - r^2)}$ where d = distance from centre.
- ✓ Incircle problems: Use tangent lengths from vertices. $AP = AS$, $BP = BQ$, etc.
- ✓ "Prove parallelogram circumscribing a circle is rhombus" — asked almost every year (5 marks).
- ✓ This is a PROOF-heavy chapter. Memorize both theorem proofs thoroughly.
- ✓ Expected marks: 5–8 marks in Board Exam.

"Practice makes perfect. Solve PYQs to master your Board Exam!"

Best Wishes for Your Board Exam!

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